



UNIVERSITY OF  
COPENHAGEN

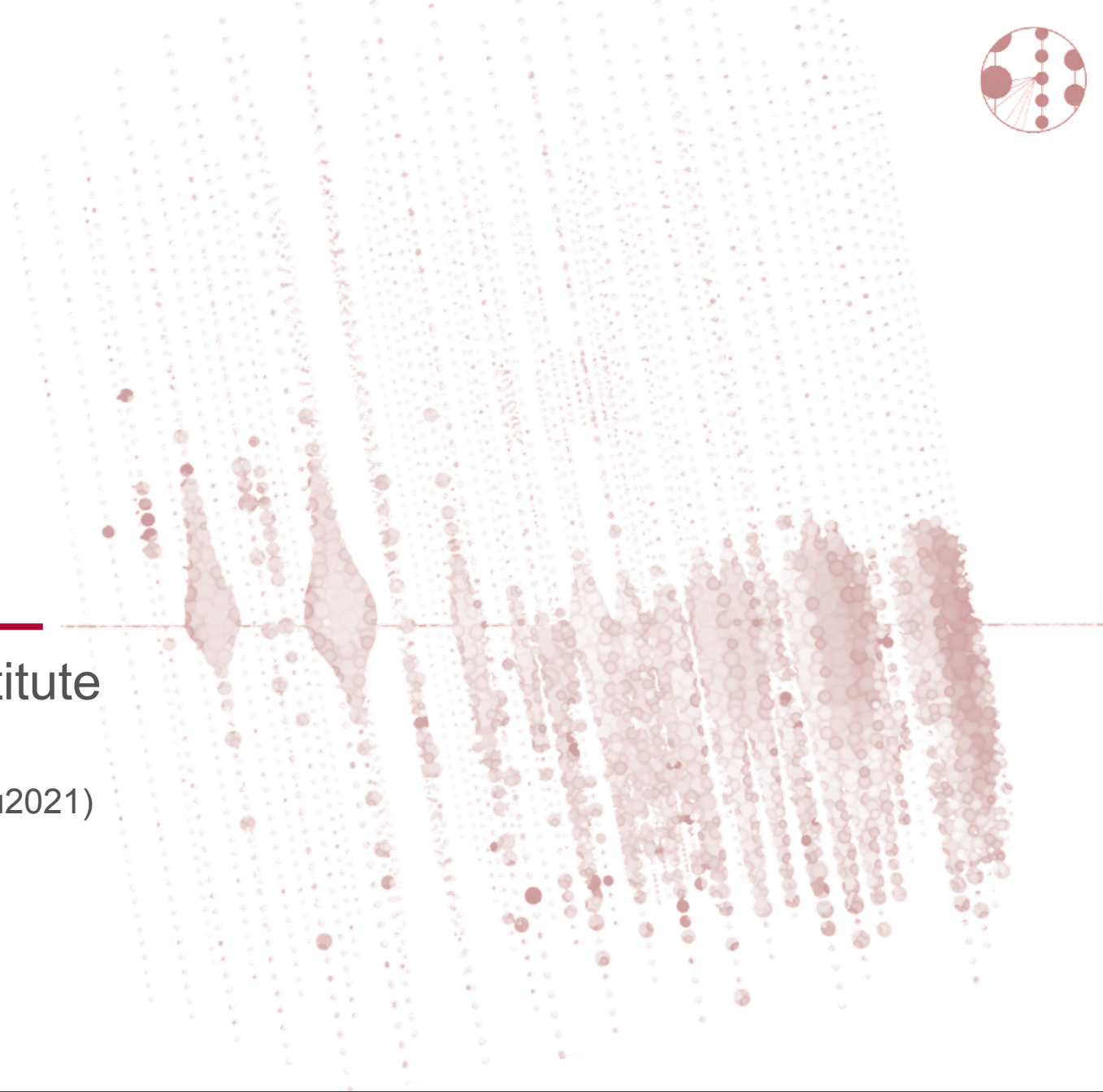


# Tau Neutrino Oscillation & IceCube

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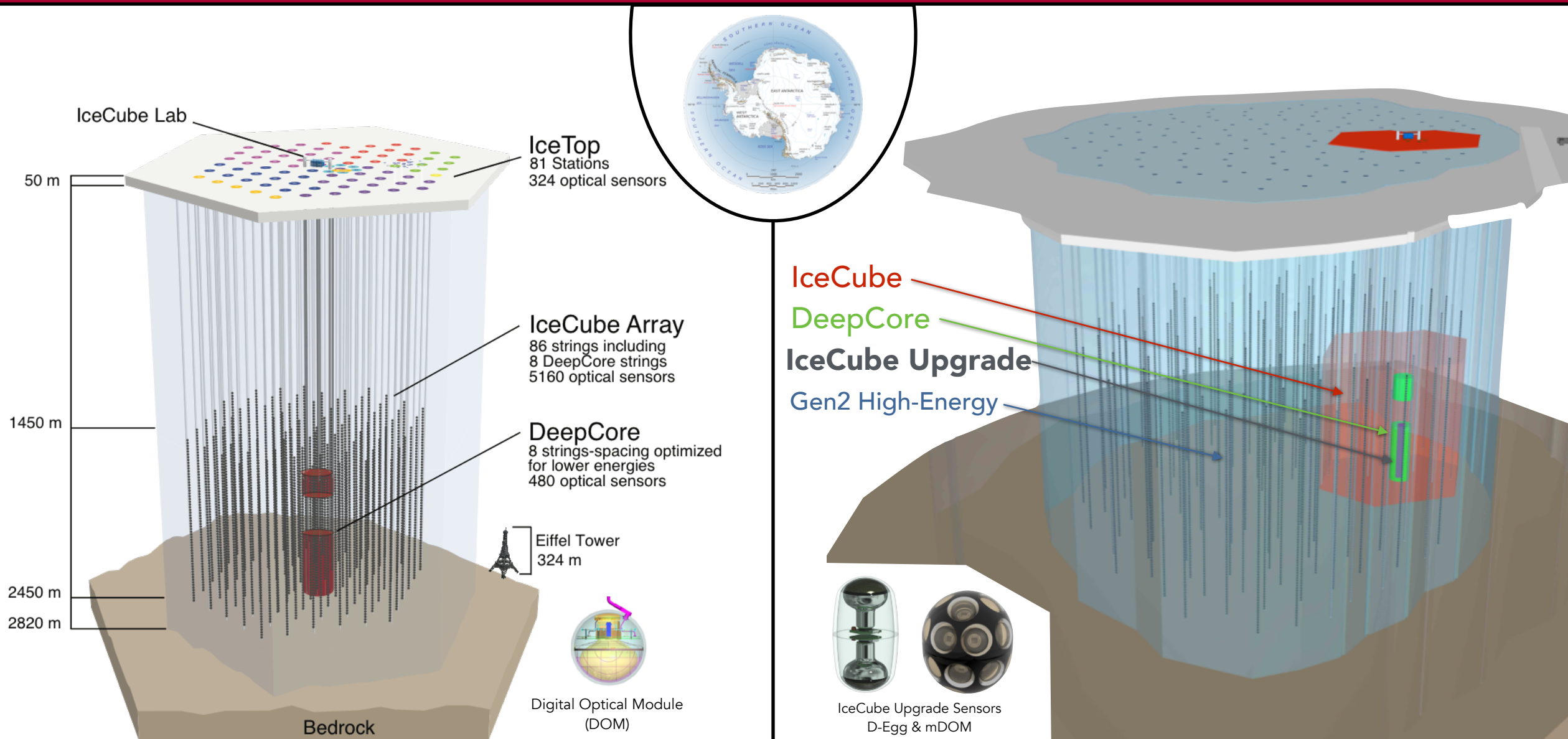
D. Jason Koskinen - Niels Bohr Institute

Workshop on Tau Neutrinos from GeV to EeV (NuTau2021)  
September 2021

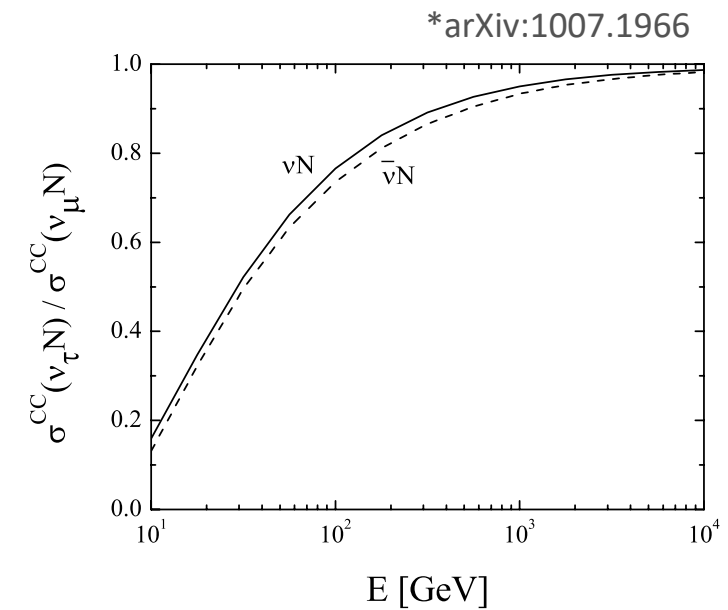
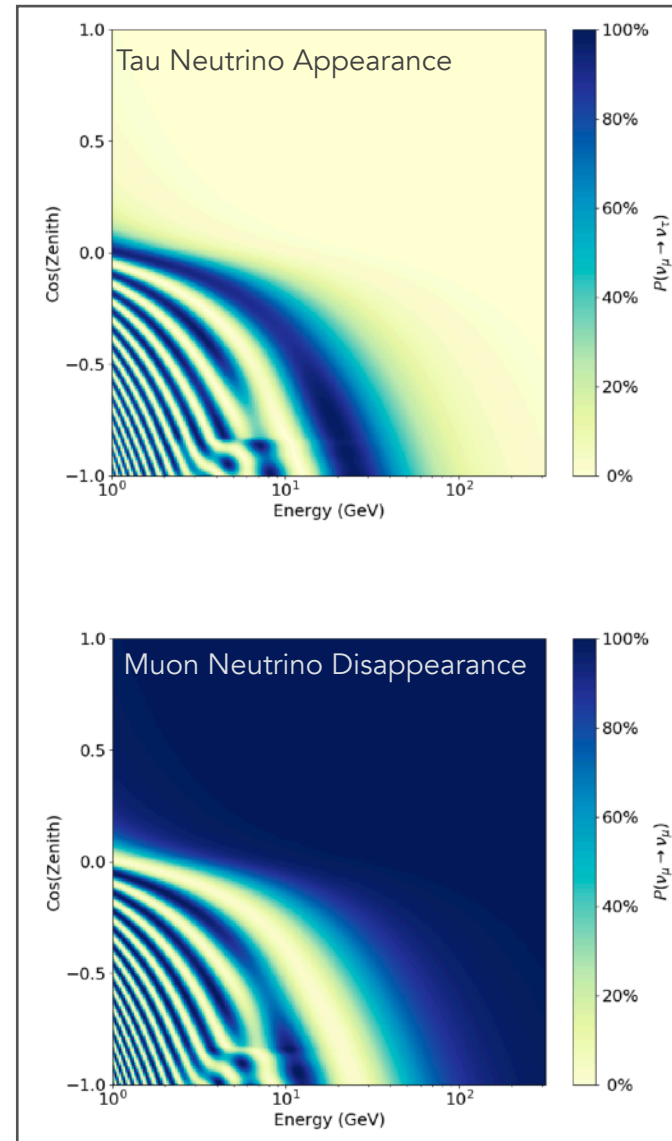
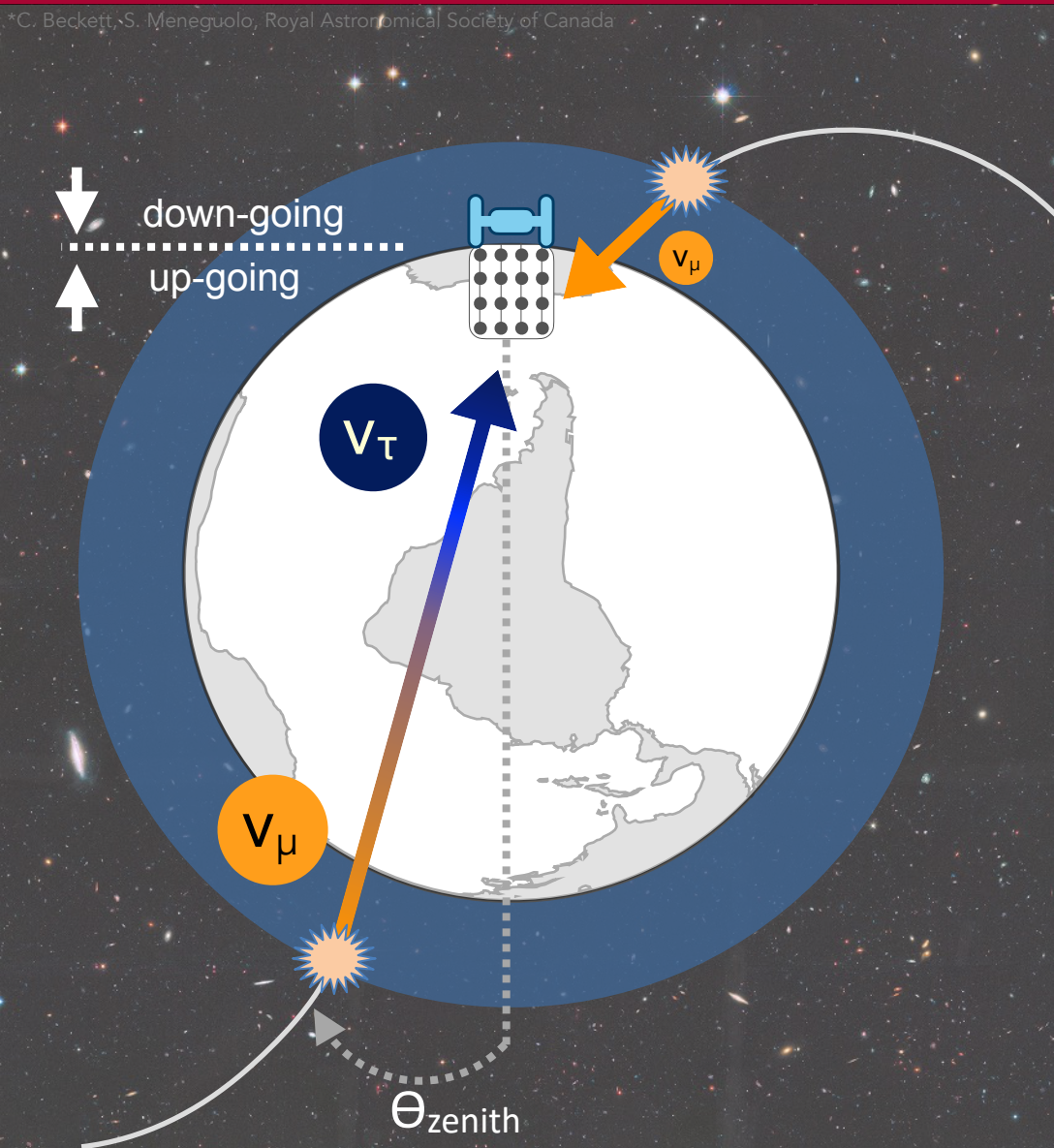


The Niels Bohr  
International Academy

# Detectors

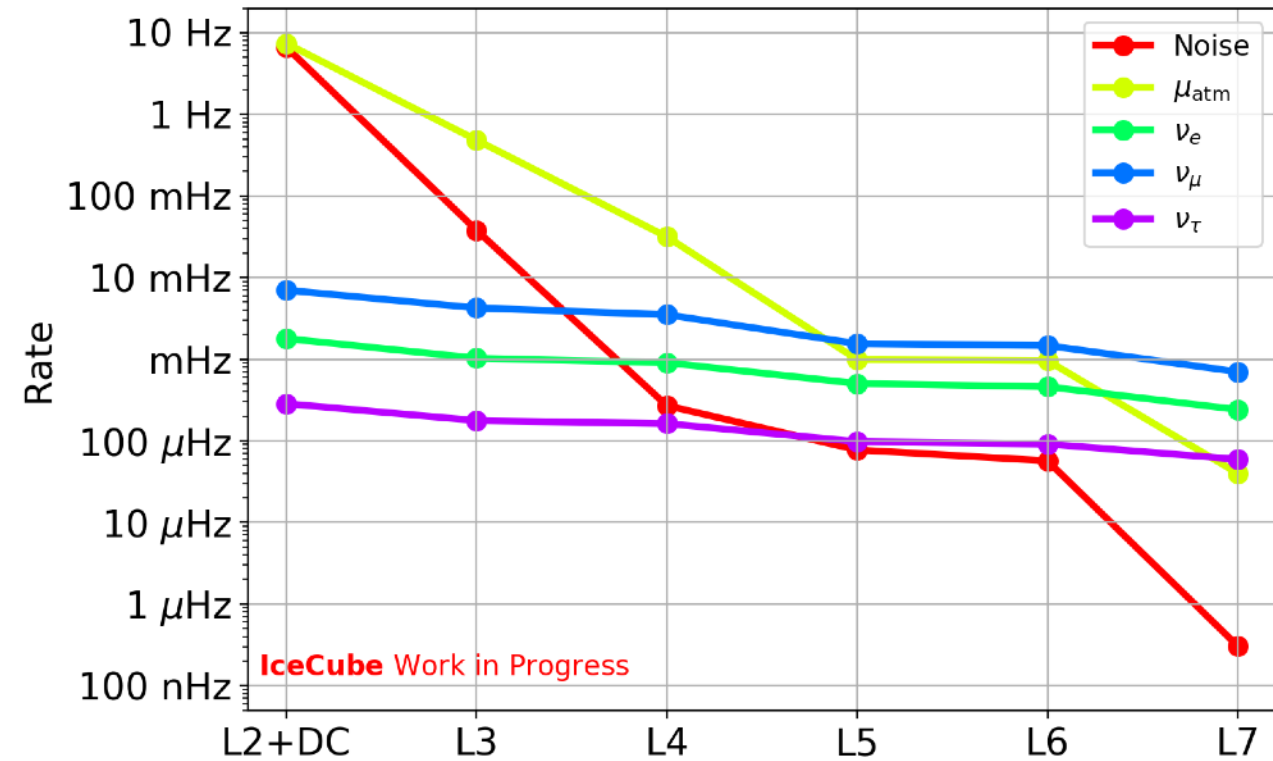


\*C. Beckett, S. Meneguolo, Royal Astronomical Society of Canada



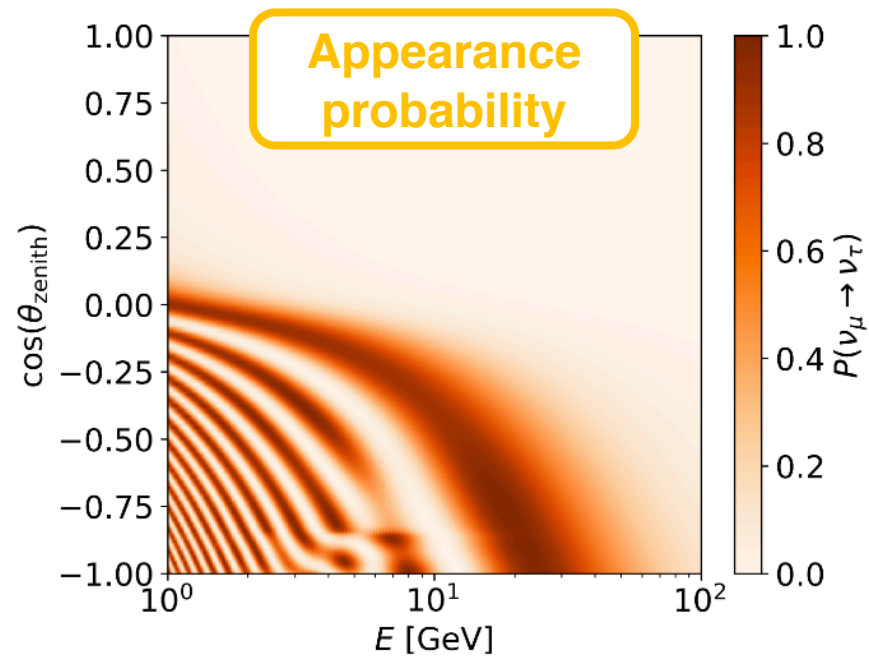


- Iterative approach to event selection
  - Backgrounds reduced by 5-7 orders of magnitude\*
    - Detector/electronics pure-noise
    - Atmospheric muons
  - Combination of straight cuts and boosted decision trees
  - Due to high event rates, the high fidelity reconstructions are introduced near end of the selection chain

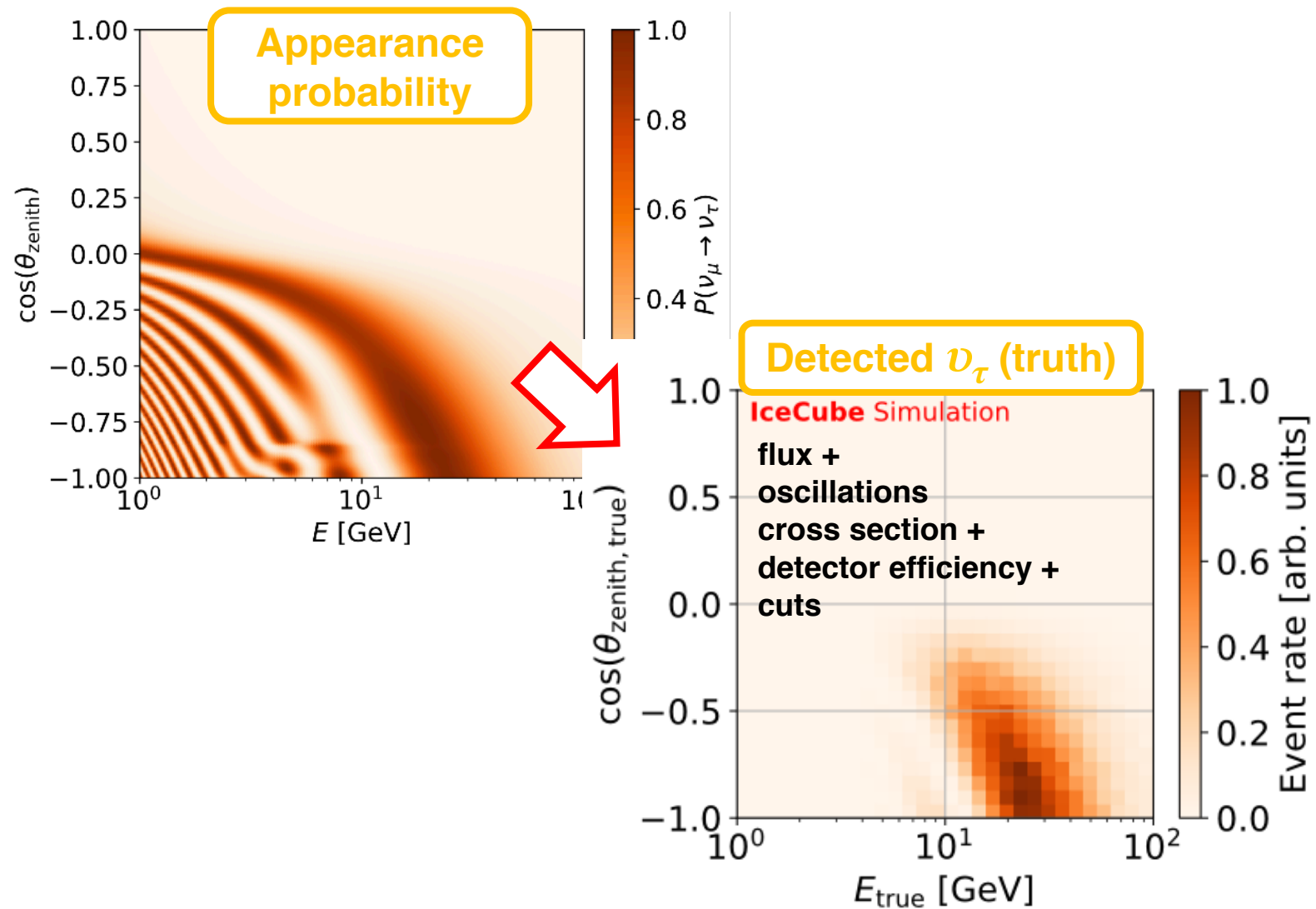


\*upcoming 8-year high-statistics event selection

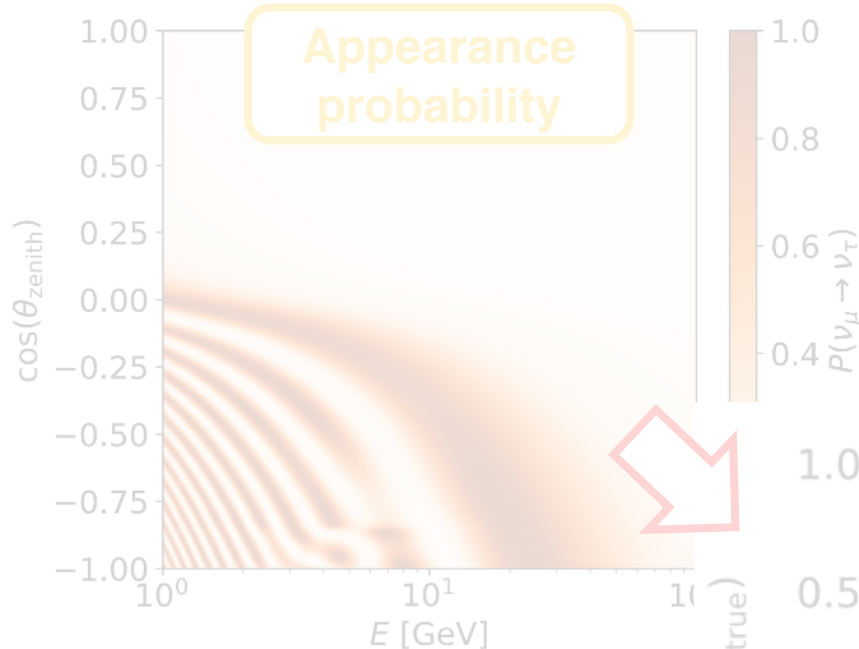
# $\nu_\tau$ appearance @ DeepCore



# $\nu_\tau$ appearance @ DeepCore



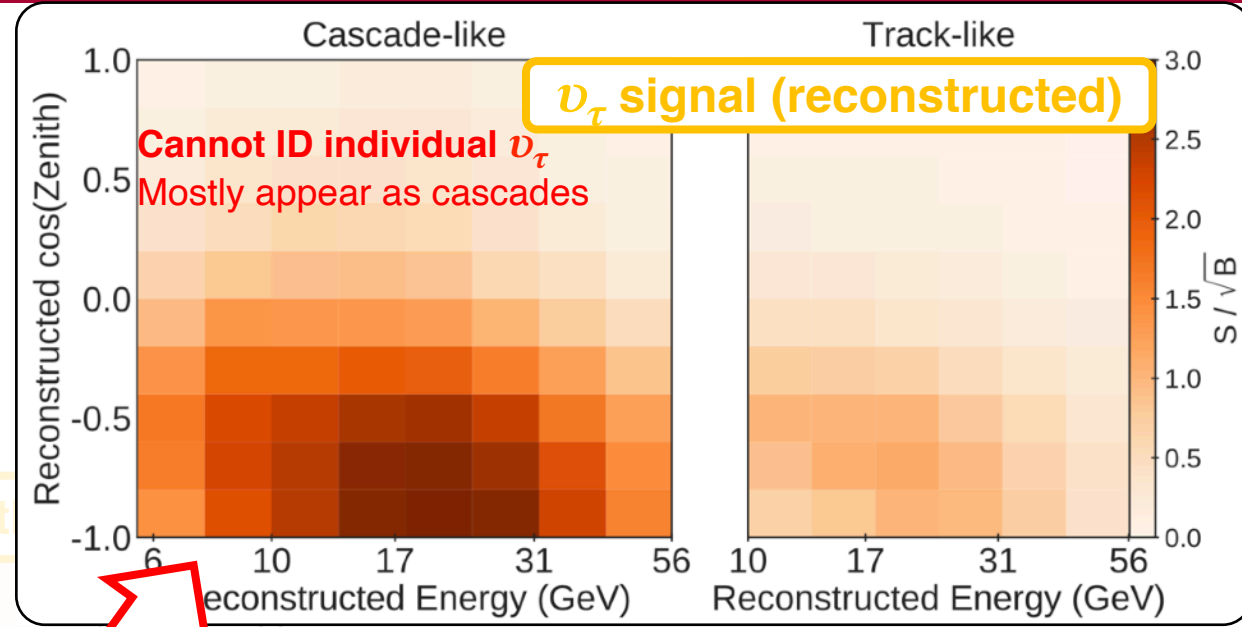
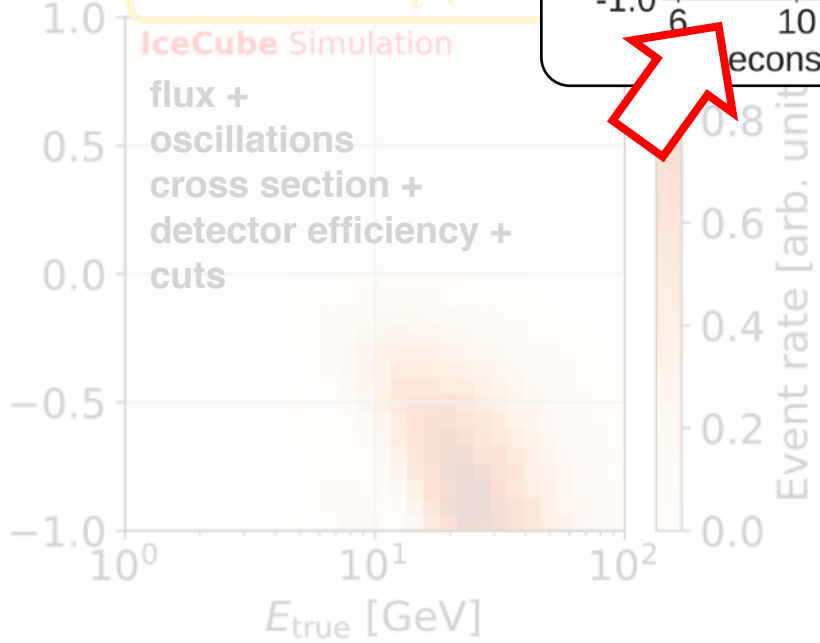
# $\nu_\tau$ appearance @ DeepCore



Detected  $\nu_\tau$  (true)

IceCube Simulation

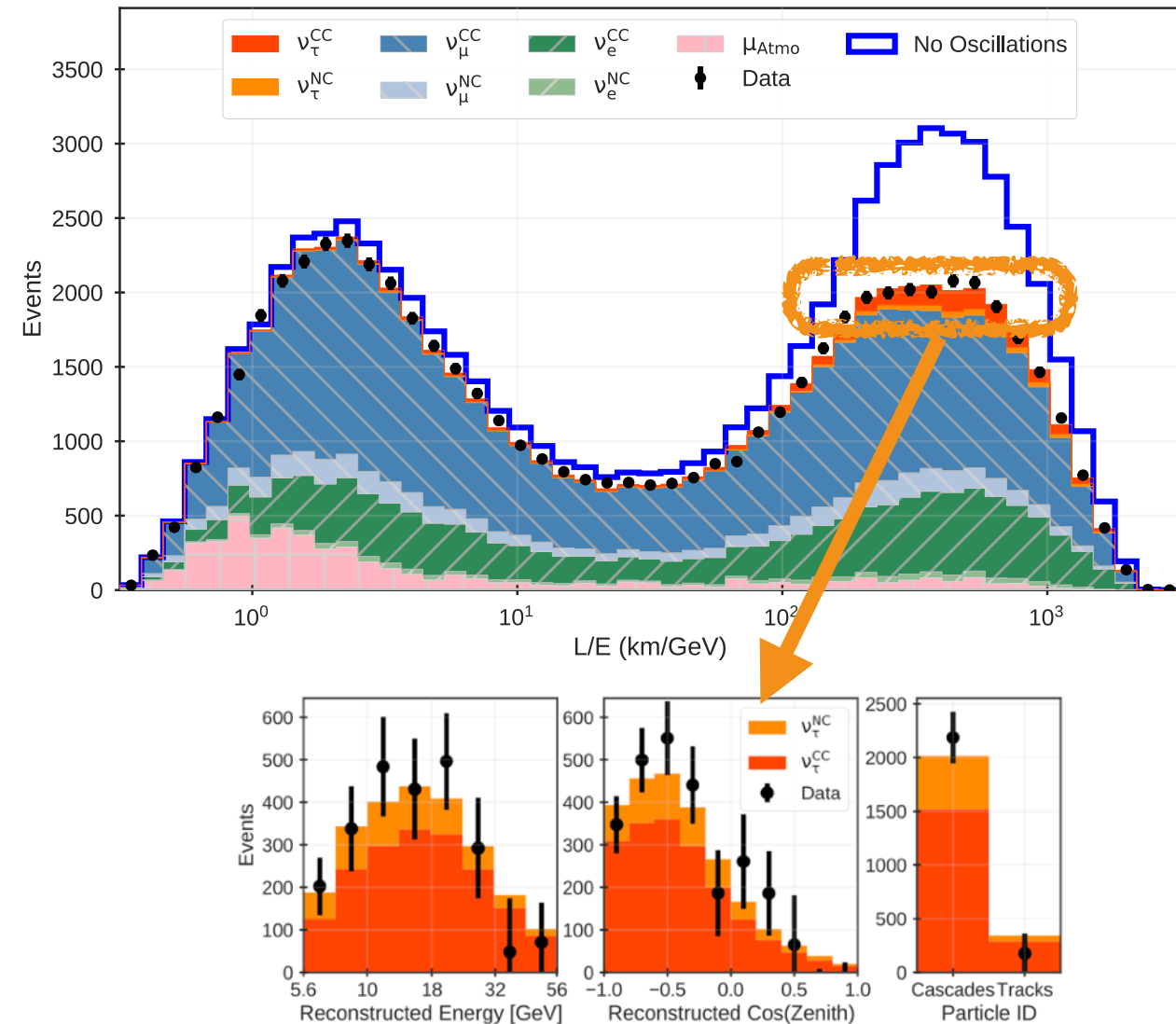
flux +  
oscillations  
cross section +  
detector efficiency +  
cuts



Statistically fit overall  $\nu_\tau$  contribution

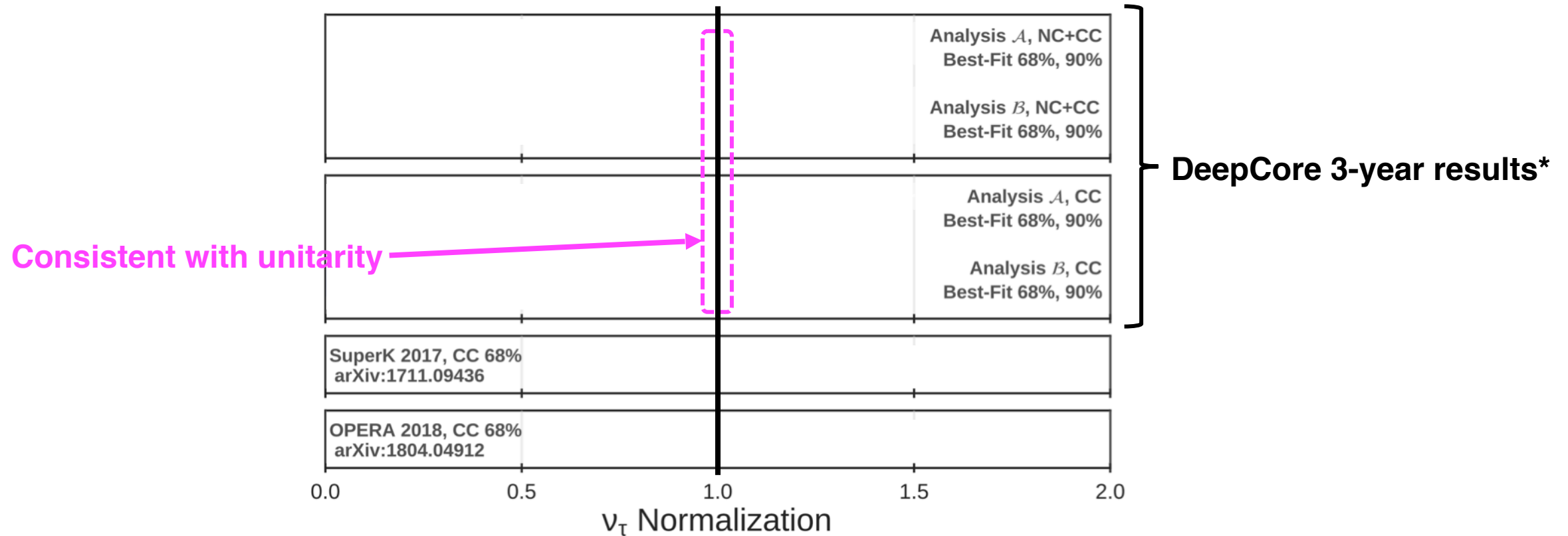
- Perform  $\nu_\mu$  disappearance fit
- Allow  $\nu_\tau$  normalisation to vary w.r.t. unitarity

- $\nu_\tau$  appearance is inclusive/  
statistical analysis
  - 3-year dataset (2018\*)
    - ~60k events, ~1.8k nutau CC
    - April 2012 - May 2015
    - 5.6 GeV - 56 GeV
  - 8-year dataset (soon)
    - ~250k events, ~10.8k nutau CC [prediction]
    - 5 GeV - 300 GeV
- Analyzed in 3 dimensions
  - Particle identification bins
    - 3-year used cascades & tracks
    - 8-year uses cascades, mixed, & tracks
  - Energy
  - Zenith (for baseline)

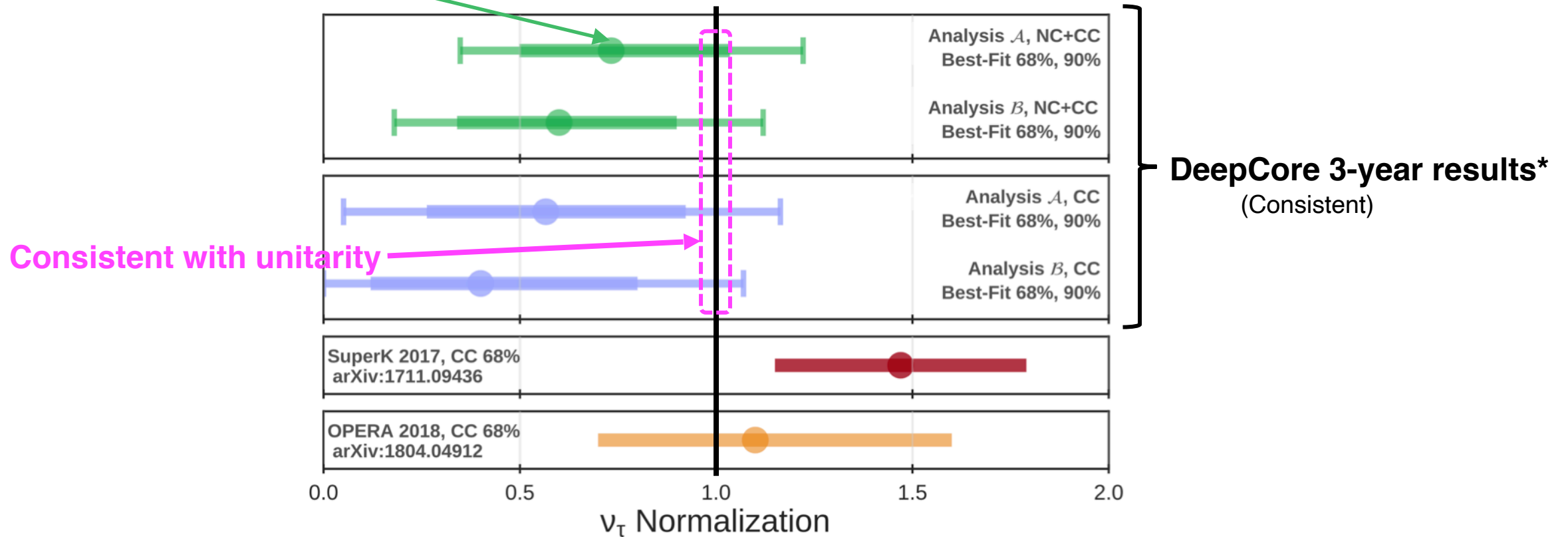


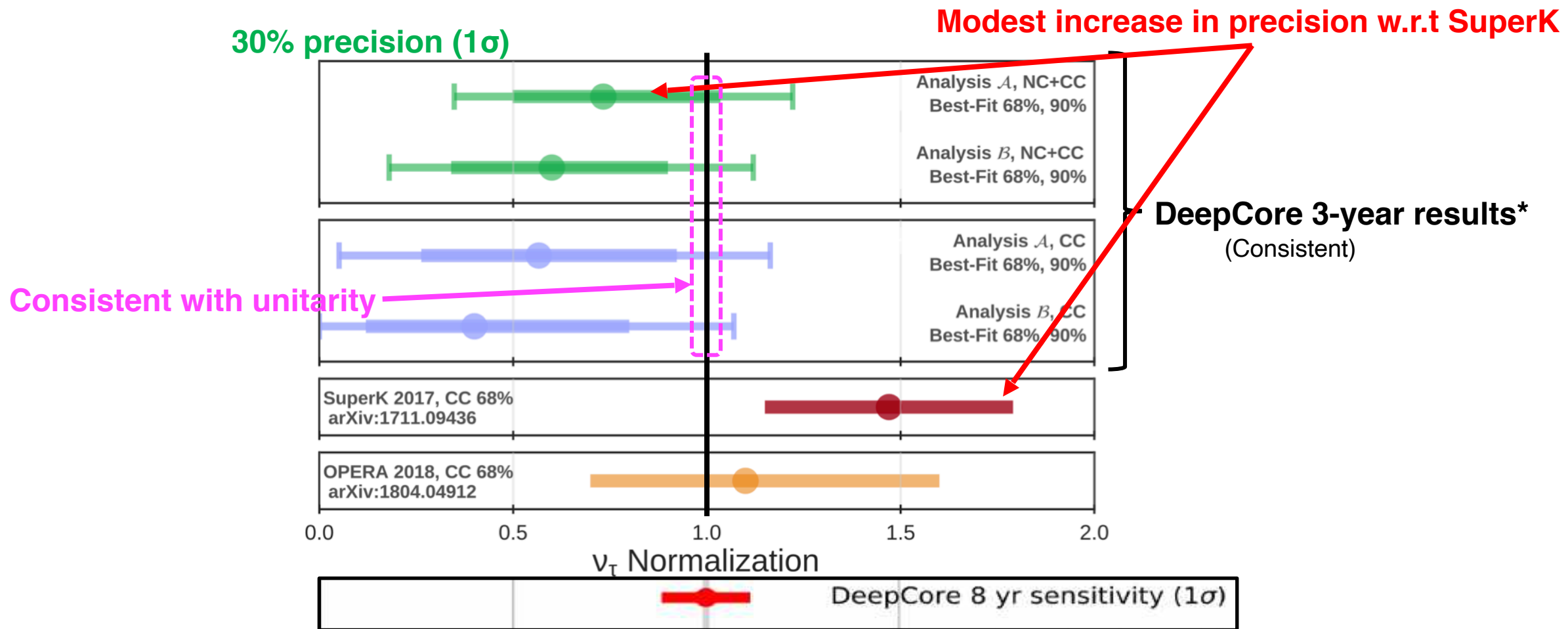
\*arXiv:1901.05366





$$N_{\nu_\tau} = 0.73^{+0.30}_{-0.24}$$



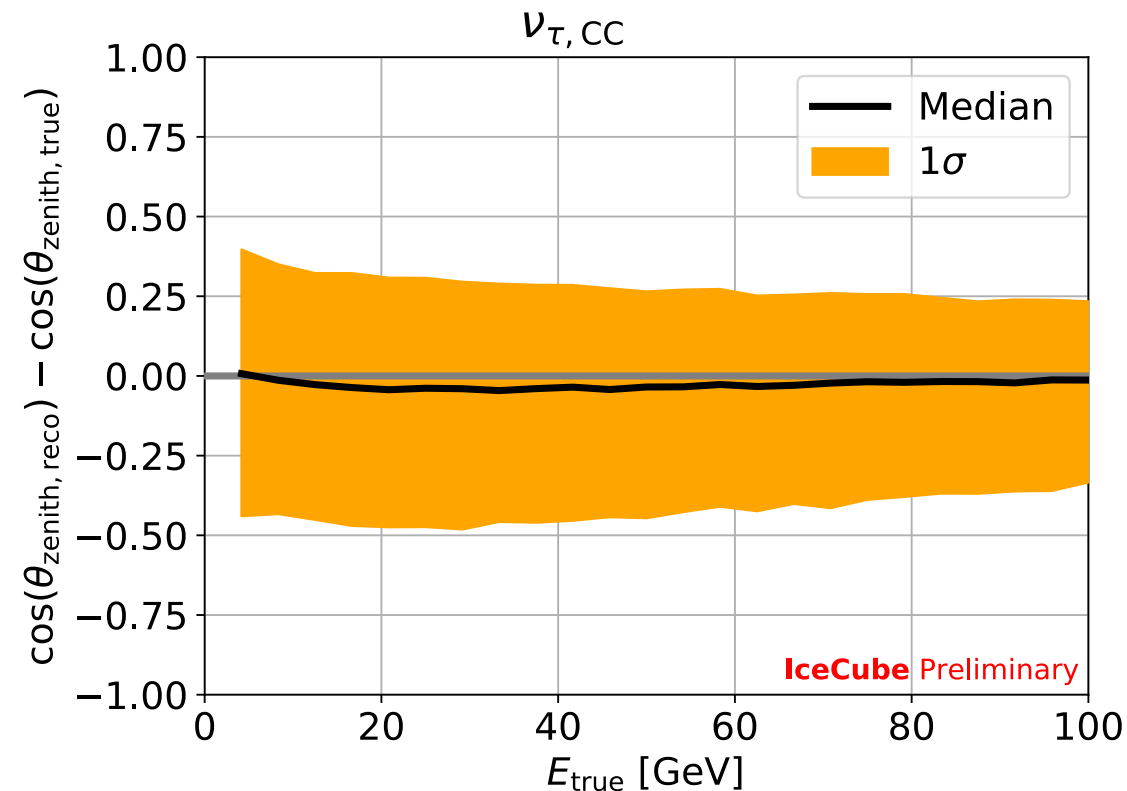


# **EXPERIMENTAL TECHNIQUES & FEATURES**

# Cascade Reconstructions ( $\nu_\tau$ )



- Previous analyses - forward light propagation
- Upcoming analysis - backwards light propagation
- Future analysis & IceCube Upgrade - likelihood free inference, convolution neural network, graph neural network
  - Faster reconstructions will provide better event selections... positive feedback loop
  - Better reconstruction resolutions are always better

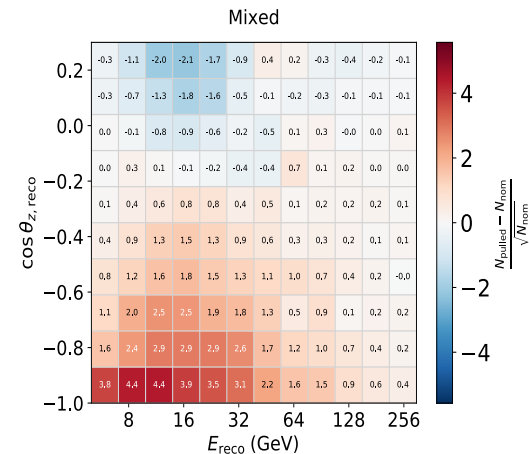
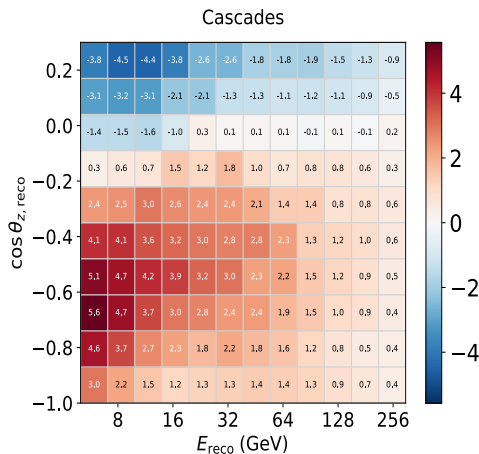




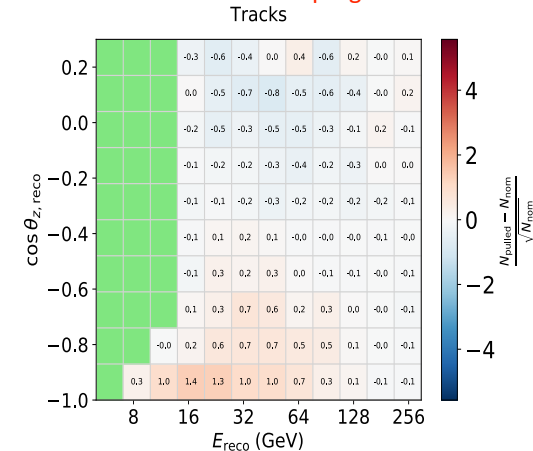
- 30+ systematic uncertainties evaluated for upcoming analysis

- Many have a negligible impact on oscillation measurements and are dropped
- The non-negligible systematics can be **very** non-negligible
  - e.g. DOM efficiency, hole ice photon scattering, spectral index
- Subset of systematics checked for  $\nu_\tau$  appearance are in backup

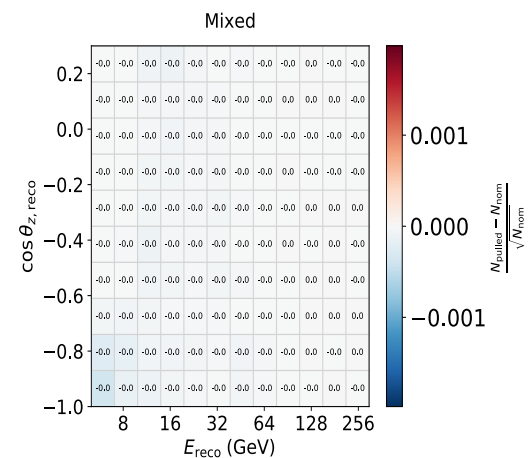
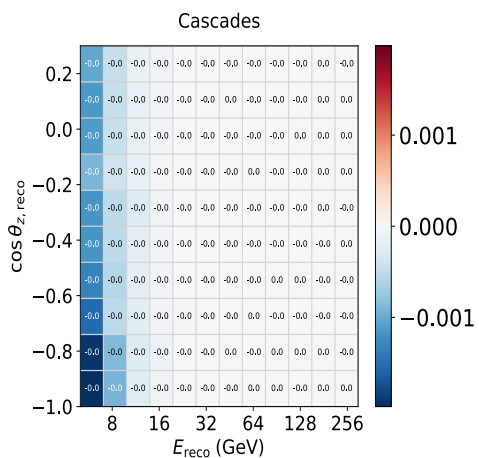
$$\Delta(\text{Hole ice, } p_0) = +0.5 : 0.102 \rightarrow 0.602$$



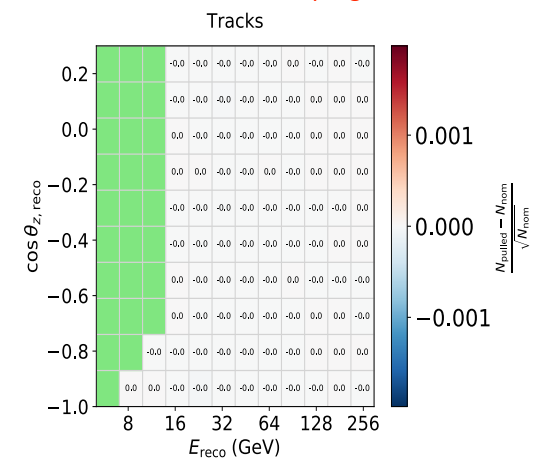
IceCube work in progress



$$\Delta(\text{Barr, } a_{\pi^+}) = -1\sigma : 0 \rightarrow -0.1$$



IceCube work in progress



\*arXiv:astro-ph/0611266

- Using ‘Barr blocks’\* for hadroproduction flux-related uncertainties
  - ~18 total
- Matrix Cascade Equation (MCEq)\*\* for flux
  - Fast and amenable to different cosmic ray spectra & hadronic interaction models
  - Correlated treatment of evolving flux particle interactions & decays

$E_i$ (GeV)	Pions				Kaons			
<8	10%			30%	40%			
8–15	30%	10%		30%	40%			
15–30	30	10	5%	10%	30	20	10%	
30–500	30	15%			40	30%		
>500	30	15%+Energy dep.			40	30%+Energy dep.		
	0	0.5		1	0	0.5		1
	$x_{LAB}$				$x_{LAB}$			

$$\frac{d\Phi}{dX} = [\hat{\Lambda}_{int} + \hat{\Lambda}_{dec}\rho^{-1}]\Phi$$

\*\*arXiv:1503.00544

- Relevant cross section uncertainties are included in analyses (DIS, RES, QE). Do we need an additional uncertainty for  $\nu_\tau$  specifically?
- Independent of kinematic considerations ( $x$ ,  $Q^2$ ,  $W$ ) or parton distribution functions, is a relative—or absolute—systematic uncertainty necessary for CC-DIS  $\nu_\tau$ , e.g.

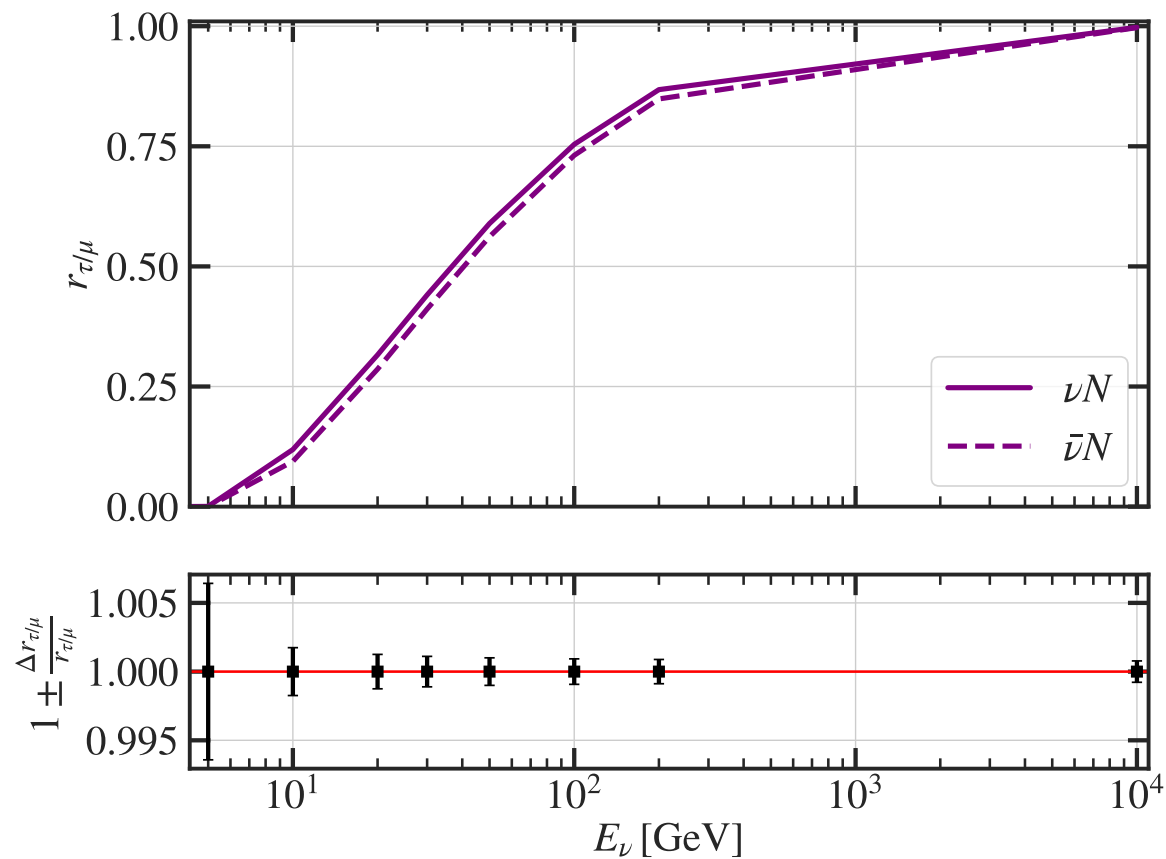
$$r_{\tau/\mu} \equiv \sigma^{\text{CC}}(\nu_\tau N) / \sigma^{\text{CC}}(\nu_\mu N)?$$

DIS cross section

$$\begin{aligned} \frac{d^2\sigma^{\nu\bar{\nu}}}{dx dy} = & \frac{G_F^2 M_N E_\nu}{\pi(1 + Q^2/M_W^2)^2} \left\{ \left( y^2 x + \frac{m_l^2 y}{2E_\nu M_N} \right) F_1(x, Q^2) + \left[ \left( 1 - \frac{m_l^2}{4E_\nu^2} \right) - \left( 1 + \frac{M_N x}{2E_\nu} \right) y \right] F_2(x, Q^2) \right. \\ & \left. \pm \left[ xy \left( 1 - \frac{y}{2} \right) - \frac{m_l^2 y}{4E_\nu M_N} \right] F_3(x, Q^2) + \frac{m_l^2 (m_l^2 + Q^2)}{4E_\nu^2 M_N^2 x} F_4(x, Q^2) - \frac{m_l^2}{E_\nu M_N} F_5(x, Q^2) \right\} \end{aligned}$$

$$r_{\tau/\mu} \equiv \sigma^{\text{CC}}(\nu_{\tau} N) / \sigma^{\text{CC}}(\nu_{\mu} N)$$

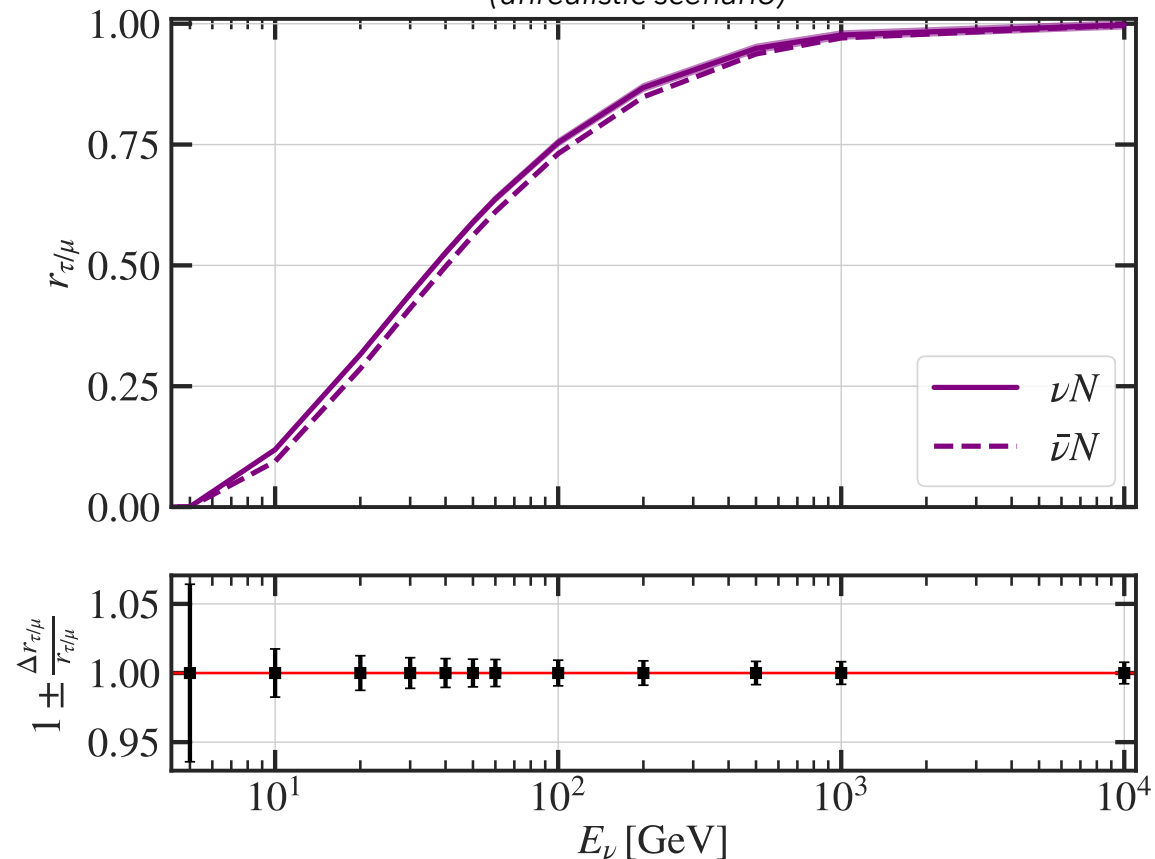
propagating 1 × the  $F_i$  uncertainties



~0.5% relative uncertainty at 5 GeV → *small!*

propagating 10 × the  $F_i$  uncertainties

(unrealistic scenario)



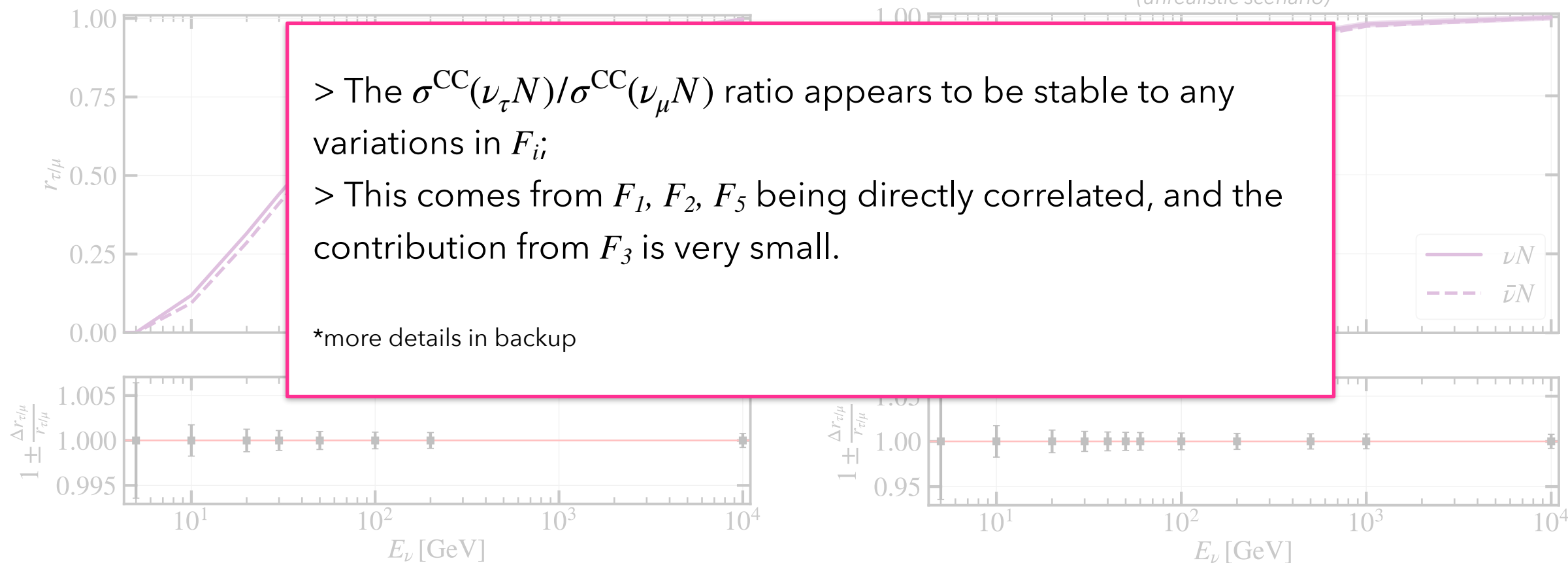
~5% relative uncertainty at 5 GeV

$$r_{\tau/\mu} \equiv \sigma^{\text{CC}}(\nu_{\tau}N)/\sigma^{\text{CC}}(\nu_{\mu}N)$$

propagating 1 × the  $F_i$  uncertainties

propagating 10 × the  $F_i$  uncertainties

(unrealistic scenario)



> The  $\sigma^{\text{CC}}(\nu_{\tau}N)/\sigma^{\text{CC}}(\nu_{\mu}N)$  ratio appears to be stable to any variations in  $F_i$

> This comes from  $F_1, F_2, F_5$  being directly correlated, and the contribution from  $F_3$  is very small.

\*more details in backup

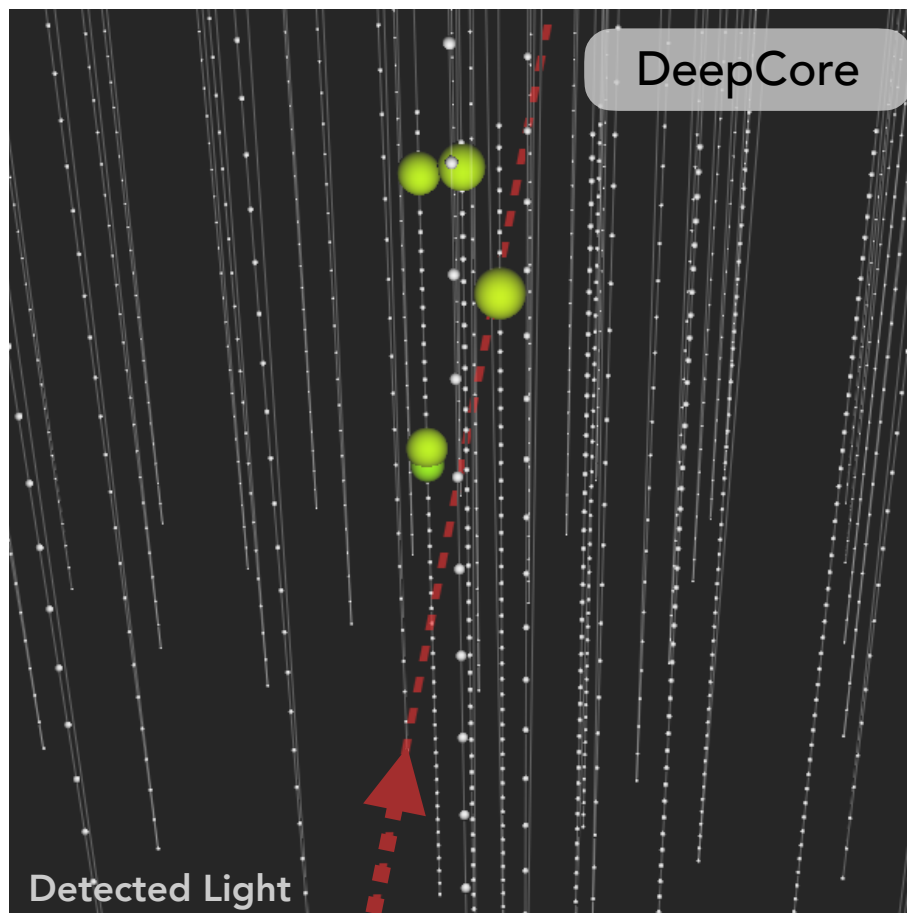
~0.5% relative uncertainty at 5 GeV → *small!*

~5% relative uncertainty at 5 GeV

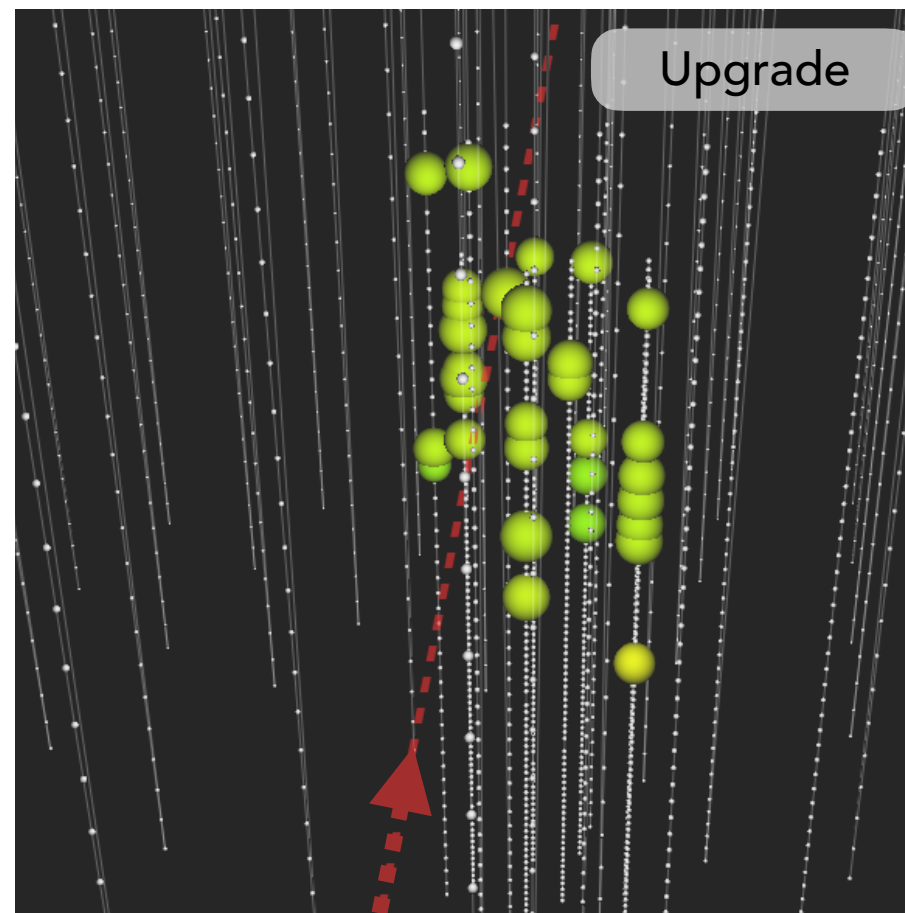


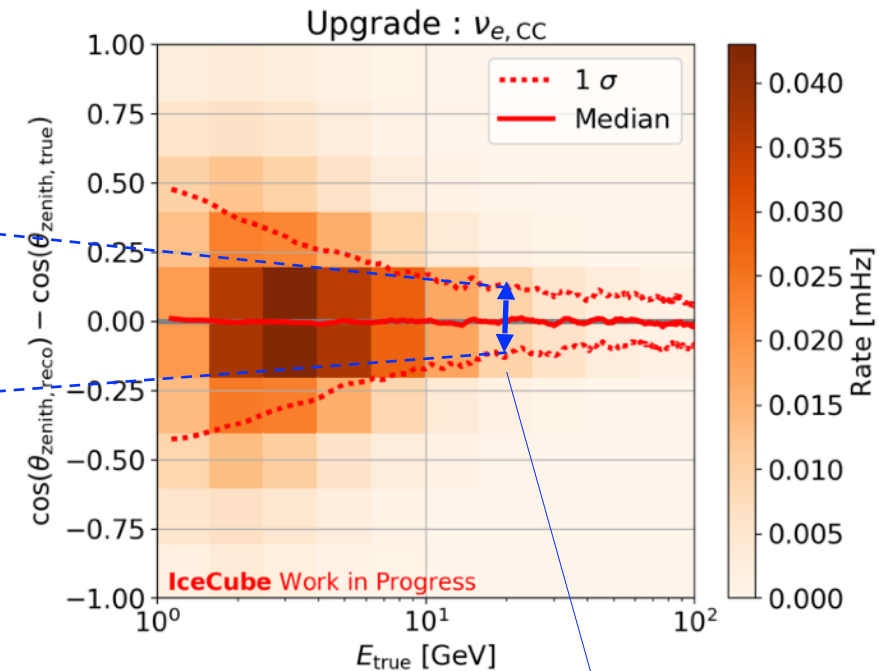
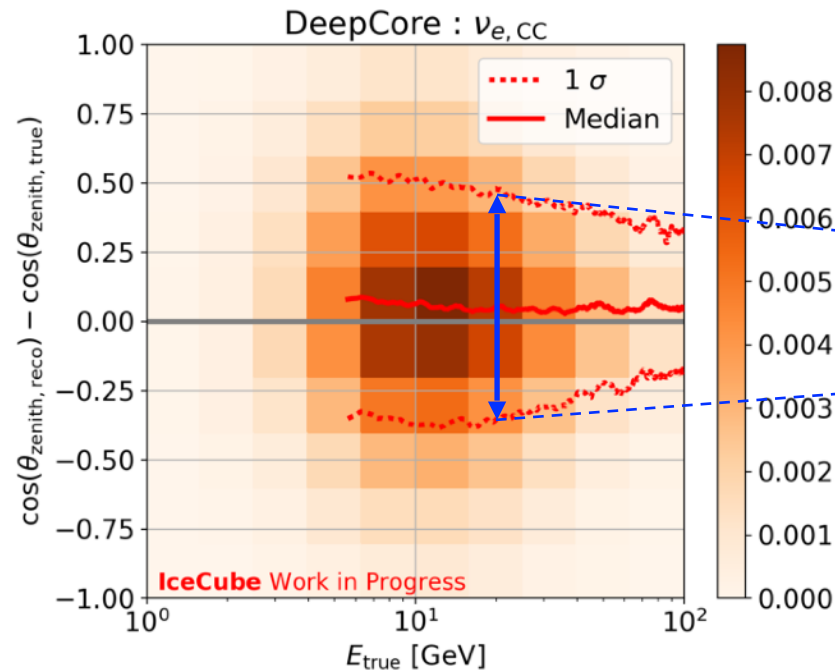
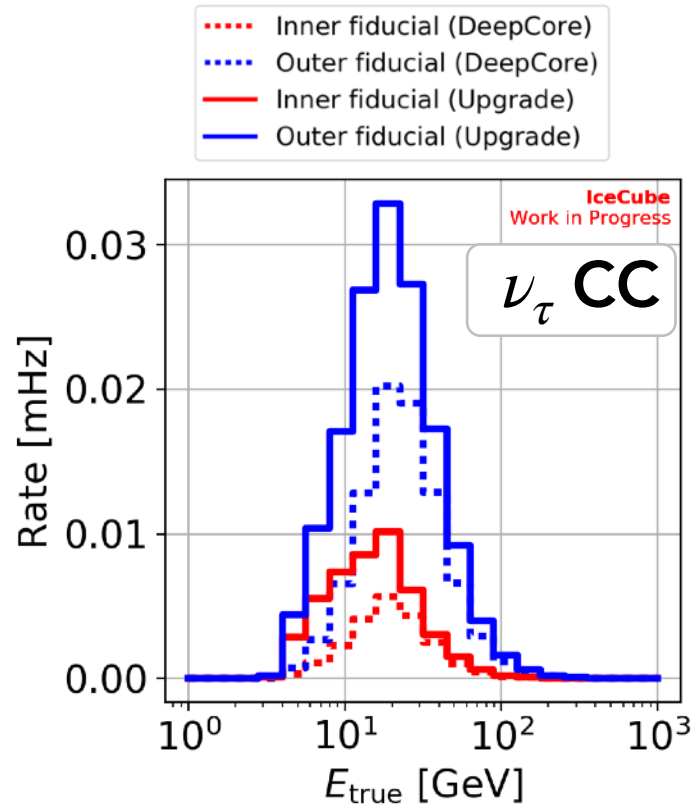
# THE FUTURE

- Dense instrumentation within inner core



29 GeV  $\nu_\tau$   
(up-going)

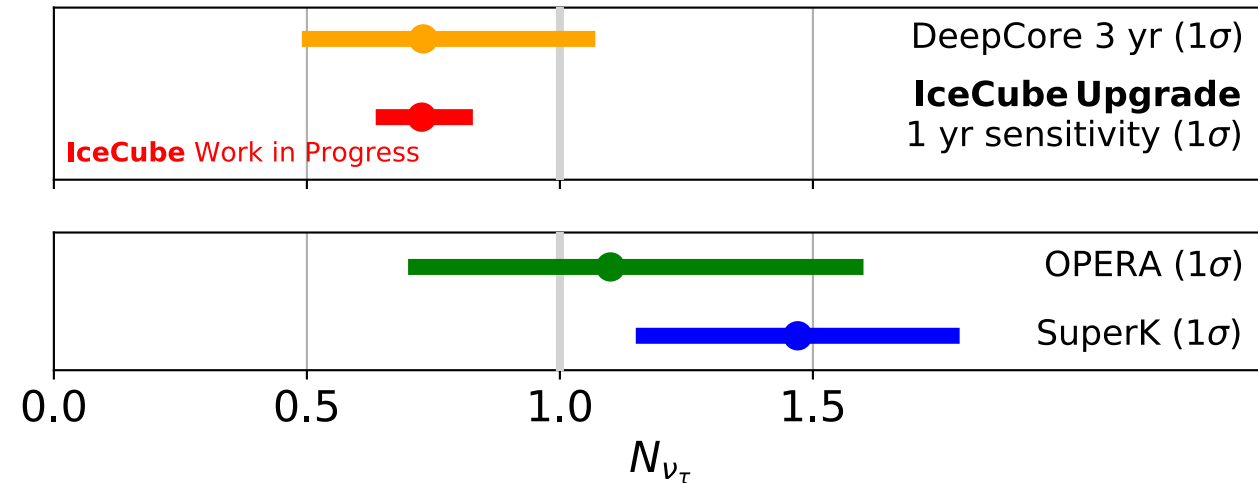




\* $\nu_e$  CC and  $\nu_{\tau}$  CC both appear as cascades.  $\nu_e$  are an easier proxy for cascade reconstruction development.

**3x improvement in cascade resolution @  $\nu_{\tau}$  appearance energies**

- Conservative experimental choices still illustrate potential of IceCube Upgrade for physics
  - $\sim 10\%$   $N_{\nu_\tau}$  resolution with 1-year of data
  - Excludes improvements from new reconstructions, better detector systematics, better flux treatment, and no combination of 10+ years of DeepCore data

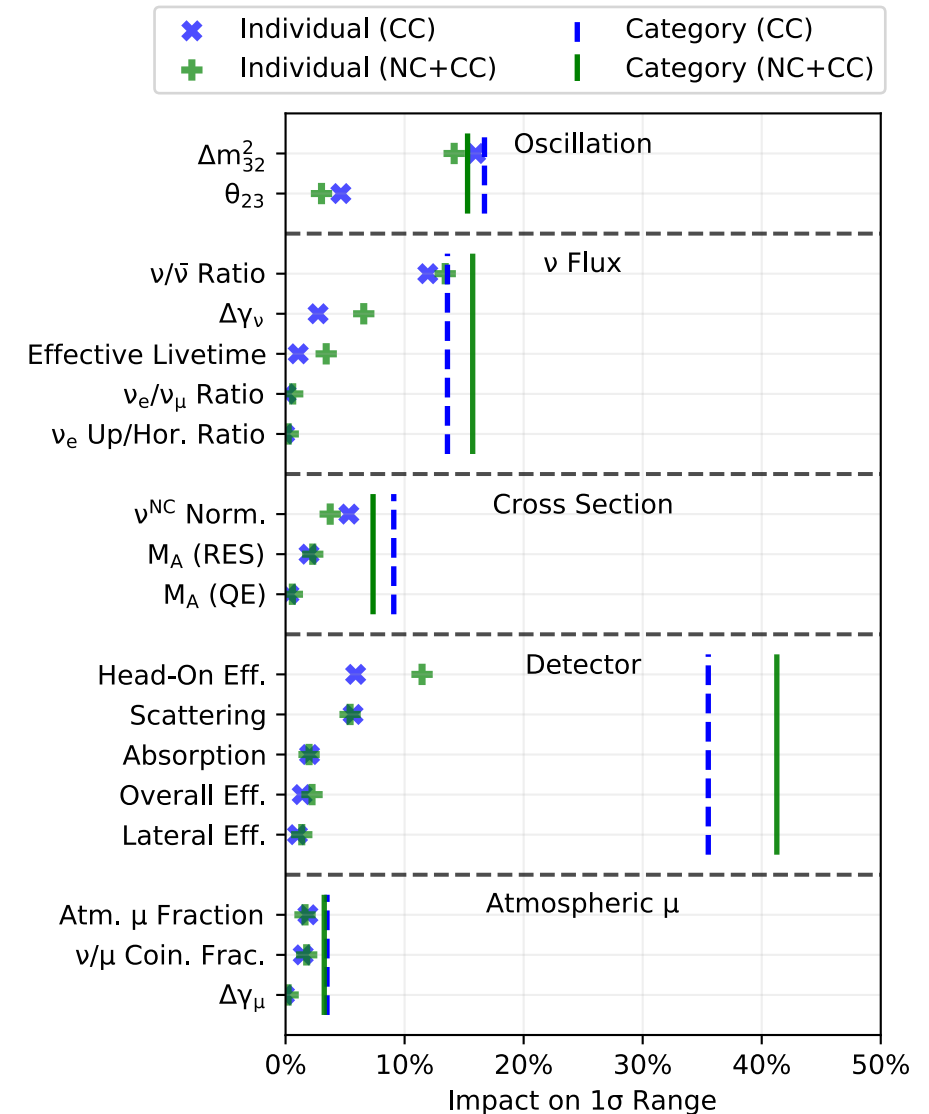


- Leading  $\nu_\tau$  appearance measurement(s) & constraints for (non)unitarity through  $N_{\nu_\tau}$
- IceCube Upgrade provides incredible future for oscillation results, notably  $\nu_\tau$



# BACKUP

- Figure is relative impact from 3-year  $\nu_\tau$  appearance analysis for the non-negligible uncertainties
- Updated list for upcoming 8-year analysis nearing finalization



# Outline of the $\nu_\tau$ xsec relative uncertainty study

1. Take the good old [Reno & Kretzer \(2002\)](#) expression for the DIS cross section:

$$\frac{d^2\sigma^{\nu/\bar{\nu}}}{dx dy} = \frac{G_F^2 M_N E_\nu}{\pi(1 + Q^2/M_W^2)^2} \left\{ \left( y^2 x + \frac{m_l^2 y}{2E_\nu M_N} \right) F_1(x, Q^2) + \left[ \left( 1 - \frac{m_l^2}{4E_\nu^2} \right) - \left( 1 + \frac{M_N x}{2E_\nu} \right) y \right] F_2(x, Q^2) \right. \\ \left. \pm \left[ xy \left( 1 - \frac{y}{2} \right) - \frac{m_l^2 y}{4E_\nu M_N} \right] F_3(x, Q^2) + \frac{m_l^2 (m_l^2 + Q^2)}{4E_\nu^2 M_N^2 x} F_4(x, Q^2) - \frac{m_l^2}{E_\nu M_N} F_5(x, Q^2) \right\}$$

2. Compute the structure functions  $F_i(x, Q^2)$ :

- 2.1. Express  $F_i(x, Q^2)$  in terms of the parton distribution functions (PDFs) for individual quarks,  $q(x, Q^2)$ ;
- 2.2. Choose a PDF set and extract the respective  $q(x, Q^2) \pm$  uncertainty.

- 3.

$$q(x, Q^2) \pm \Delta q(x, Q^2) \rightarrow F_i(x, Q^2) \pm \Delta F_i(x, Q^2) \rightarrow \sigma_l(E) \pm \Delta \sigma_l(E) \rightarrow \frac{\sigma_{\nu_\tau}(E)}{\sigma_{\nu_\mu}(E)} \pm \Delta \left( \frac{\sigma_{\nu_\tau}(E)}{\sigma_{\nu_\mu}(E)} \right)$$

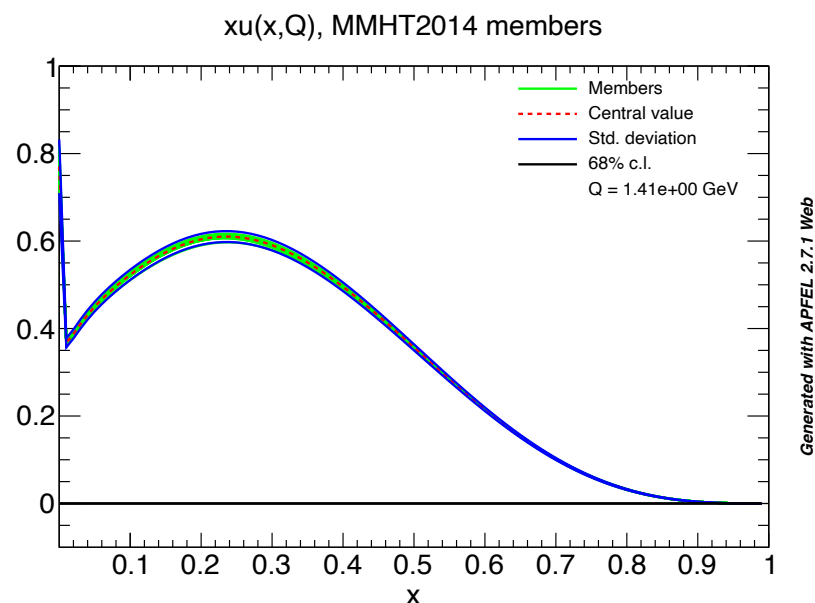
# 2.1. Computing the structure functions

$u(x), c(x) \dots$  etc. are PDF-specific

proton target	$F_{2p}^\nu(x) = 2x[d(x) + s(x) + \bar{u}(x) + \bar{c}(x)]$ $xF_{3p}^\nu(x) = 2x[d(x) + s(x) - \bar{u}(x) - \bar{c}(x)]$	$F_{2p}^{\bar{\nu}}(x) = 2x[u(x) + c(x) + \bar{d}(x) + \bar{s}(x)]$ $xF_{3p}^{\bar{\nu}}(x) = 2x[u(x) + c(x) - \bar{d}(x) - \bar{s}(x)]$
neutron target	$F_{2n}^\nu(x) = 2x[u(x) + s(x) + \bar{d}(x) + \bar{c}(x)]$ $xF_{3n}^\nu(x) = 2x[u(x) + s(x) - \bar{d}(x) - \bar{c}(x)]$	$F_{2n}^{\bar{\nu}}(x) = 2x[d(x) + c(x) + \bar{u}(x) + \bar{s}(x)]$ $xF_{3n}^{\bar{\nu}}(x) = 2x[d(x) + c(x) - \bar{u}(x) - \bar{s}(x)]$
isoscalar target	$F_{iN} = \frac{F_{ip} + F_{in}}{2} \quad \leftarrow \text{assumed in this work}$	
leading order relations	$F_1(x) = F_5(x) = \frac{F_2(x)}{2x}; F_4(x) = 0.$	

# 2.2. Accessing the individual quark PDFs

> The [LHAPDF](#) database provides the PDF sets with measurements & fits from different groups, for example:



- > Several Python libraries (such as [parton](#) or [pdfflow](#)) can process these files directly and extract the PDFs for a needed flavor;
- > The central value is normally “member 0”;
- > The confidence limits (68 or 90%, stated in the info file) are given in the other “members” of the PDF set.

## LHAPDF 6.3.0

Main page	PDF sets	Class hierarchy	Functions	Examples	More...
PDF sets					

Official [LHAPDF 6.3](#) PDF sets: currently 1045 available, of which 1044 are validated.

LHAPDF ID	Set name and links	Number of set members	Latest data version	Notes
251	GRVP10 <a href="#">(tarball)</a> <a href="#">(info file)</a>	1	1	alpha_s was broken in LHAPDF5. This version uses approximate 1st order running from reported Lambda4,5 values.
252	GRVP11 <a href="#">(tarball)</a> <a href="#">(info file)</a>	1	1	
270	xFitterPI_NLO_EIG <a href="#">(tarball)</a> <a href="#">(info file)</a>	8	1	
280	xFitterPI_NLO_VAR <a href="#">(tarball)</a> <a href="#">(info file)</a>	6	1	
10000	cteq6 <a href="#">(tarball)</a> <a href="#">(info file)</a>	41	-1	Corresponds to LHAPDF5's cteq6 or cteq6mE; central member equivalent to cteq6m.
10042	cteq6l1 <a href="#">(tarball)</a> <a href="#">(info file)</a>	1	4	
10150	cteq61 <a href="#">(tarball)</a> <a href="#">(info file)</a>	41	1	
10550	cteq66 <a href="#">(tarball)</a> <a href="#">(info file)</a>	45	1	



### 3. Building up the cross sections: $d\sigma/dy$

> Plugging the  $F_i$  into the DIS cross section formula, we get the following differential cross sections:

> The shapes and the relative scaling between the flavours are ~in agreement with those from Reno (right panel).

